

BJS Federation of Schools

Calculation Policy

Policy Adopted: Spring 2022

Dantoen

Signed: ______ Ms A. Parker Executive Headteacher

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Introduction

1. The Calculation Policy has been put together in consultation with the staff at the BJS Partnership. All staff should refer to the policy in order to provide continuity and development in written calculations as children progress through the schools.

1.1 This policy brings together our ideas and practice in striving to provide our children with every opportunity to achieve in mathematics.

2. Aims:

- To raise attainment and increase pupil progress
- To have a consistent approach to the teaching of calculations throughout the school
- To ensure progression between classes and across the Key Stages
- To provide all teaching and support staff with a framework for the teaching of calculation strategies in line with the Maths Mastery approach.

3. How to use this policy:

- Use the policy as the basis of your planning but ensure you use previous or following years' guidance to allow for personalised learning
- Always use Assessment for Learning to identify suitable next steps in calculation for groups of children
- If, at any time, children are making significant errors, return to the previous stage in calculation
- Always use suitable resources, models and images to support children's understanding of calculation and place value, as appropriate
- Encourage children to make sensible choices about the methods they use when solving problems

3.1 This policy has been designed to teach children through the use of concrete, pictorial and abstract representations (CPA).

3.2 Concrete representation: a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.

3.3 Pictorial representation: a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.

3.4 Abstract representation: a pupil is now capable of representing problems by using mathematical notation, for example $12 \times 2 = 24$.

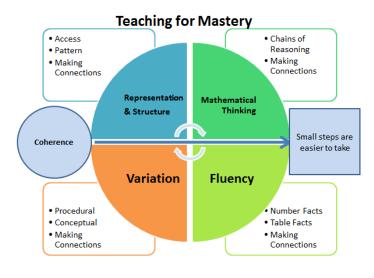
3.5 It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations. It is also worth noting that if a child has moved on from the concrete to the pictorial, it does not mean that the concrete cannot be used alongside the pictorial. Or, if a child is working in the abstract,

'proving' something or 'working out' could involve use of the concrete or pictorial. Similarly, although the strategies are taught in a progressive sequence, they are designed to equip children with a 'tool box' of skills and strategies that they can apply to solve problems in a range of contexts. So, as a new strategy is taught, it does not necessarily supersede the previous, but builds on prior learning to enable children to have a variety of tools to select from. As children become increasingly independent, they will be able to, and must be encouraged to, select those strategies which are most efficient for the task.

4. Mastery in Mathematics

4.1 At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations.

4.2 Procedural fluency and conceptual understanding are developed in tandem because each supports the development of the other.



5. Mathematical Language

The 2014 National Curriculum is explicit in articulating the importance of children using the correct mathematical language as a central part of their learning (reasoning). In certain year groups, the non-statutory guidance highlights the requirement for children to extend their language around certain concepts. It is therefore essential that teaching using the strategies outlined in this policy is accompanied by the use of appropriate and precise mathematical vocabulary. New vocabulary should be introduced in a suitable context (for example, with relevant, real objects, apparatus, pictures of

diagrams) and explained carefully. High expectations of the mathematical language used are essential to close the vocabulary gap and ensure the children have mathematical cultural capital.

YEAR 1 - ADDITION

Objective:	CPA:				
Combining two parts to make a whole number.	CrA. Concrete: Use cubes to add two numbers together as a group or a bar. Pictorial: Use pictures to add two numbers together as a group or in a bar. Pictorial: Use pictures to add two numbers together as a group or in a bar.				
	4 + 3 = 7 10 = 6 + 4 Empty box with numerals $4 + \prod is 7$				
Starting at the bigger number and counting on.	Concrete: Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer. Progress to using a number line or track to count on. Eg. 4+ 2 = 6 0 1 2 3 4 5 6 7 8 9 10 Pictorial: Start at the larger number on the number line and count on in ones or in one jump to find the answer. Eg. 12 + 5 = 17 Once children are confident with using a marked number line, introduce an empty number line to count on. Eg. 6 + 3 = Abstract: Place the larger number in your head				

	and count on the smaller number to find your answer.				
	Mental strategies to solve simple problems in addition and encourage children's own recording using conventional signs.				
Adding three single digit numbers (make ten first)	Concrete: Pupils may need to try different combinations before they find the two numbers that make 10. Eg. 4 + 7 + 6 = The first bead string shows 4, 7 and 6. The colours of the bead string show that it makes more than ten. The second bead string shows 4, 6 and then 7. The final bead string shows how they have now been put together to find the total. Pictorial: Progress to using part-part-part whole model. Abstract: 3p + [] + 1p = 8p 3+4+2= [] 4 + 7 + 6 = 10 + 7 = 17				
Regrouping ten ones to make ten. (this is an essential skill that will support column addition later on)	Concrete: Start with the bigger number and use the smaller number to make 10. Pupils should be encouraged to start at the greater number and partition the smaller number tomake ten. The colours of the beads on the bead string make it clear how many more need to be added to make ten. Also, the empty spaces on the ten frame make it clear how many more are needed to make ten. Pictorial: Use pictures or a number line. Regroup or partition the smaller number to make 10. Pictorial: Use pictures or a number line. Regroup or partition the smaller number to make 10. 4 + 9 = 3 + 9 = 12				

	9 + 5 = 14 $1 4$ $+1$ $+4$ $1 4$ $+1$ $+1$ $+4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ $1 + 4$ $1 + 1$ 1			
	Abstract: 7 + 4 = 11			
	"If I am at seven, how many more do I need to make 10? How many more do I add on now?"			
	Children are encouraged to use full sentences and support children using language structures on slides.			
Represent & use number	Concrete:			
bonds and related subtraction facts within	E. 2 more than 5			
20.	Pictorial:			
	යි යි මි ම ම ම ම ම ම ම ම ම ම ම ම ම ම ම ම			
	Abstract: Emphasis should be on the language:			
	"1 more than 5 is equal to 6" "2 more than 5 is 7"			
	"8 is 3 more than 5"			
	Over time, pupils should be encouraged to rely more on their number bonds knowledge than counting strategies.			

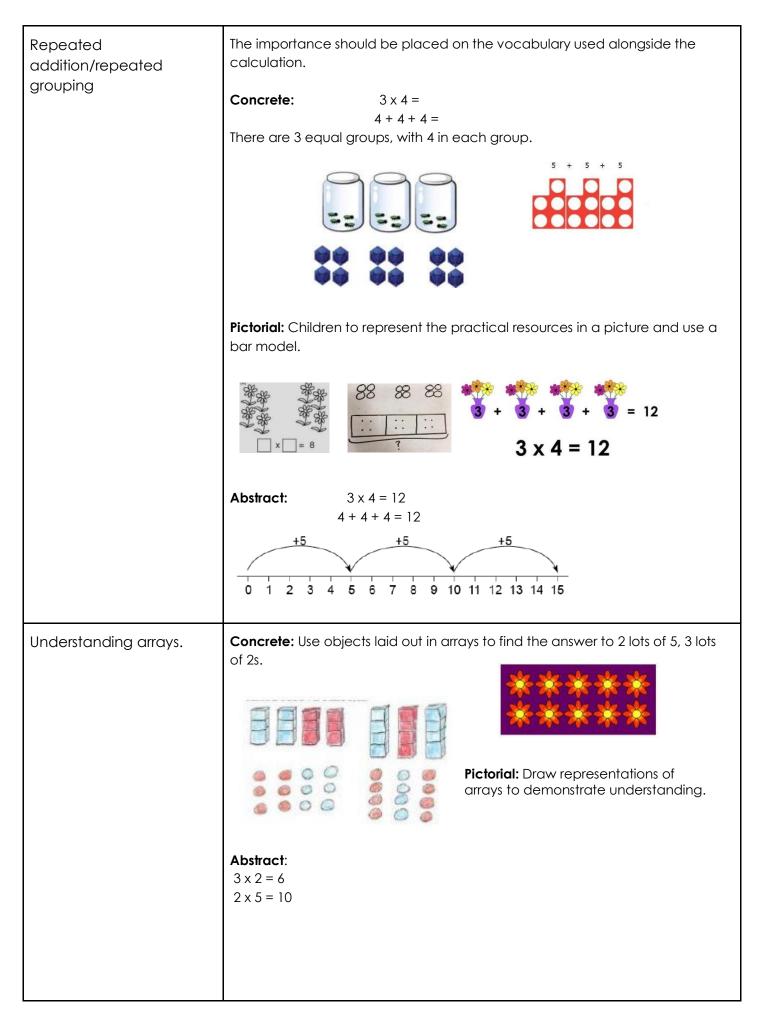
YEAR 1 - SUBTRACTION

Objective:	CPA:				
Taking away from the ones.	Concrete: Use physical objects, counters, cubes etc, to show how objects can be taken away.				
	Pictorial: Cross out drawn objects to show how many have been taken away. The bar model can also be used.				
Counting back.	Pupils should be encouraged to rely on number bond knowledge as time goes on, rather than using counting back as their main strategy. Concrete: Counting back (using number lines or number tracks) children start with 6 and count back 2.				
	Pictorial: Children represent what they see pictorially. Abstract: Children represent the				
	$\begin{array}{c} 12 13 13 15 10 17 18 \\ \hline \\ 4 5 6 7 \end{array}$ calculation on a number line or number line track and show their jumps. Encourage children to use an empty number line.				

Finding the difference	Concrete: Finding the difference using cubes, Numicon, or other objects.				
	Calculate the difference between 8 and 5:				
	Pictorial: Children draw the cubes/other concrete objects which they have used or use the bar model to illustrate what they need to calculate.				
	Abstract: Find the difference between 8 and 5.				
	8 - 5, the difference is				
	Children to explore why				
	9 - 6 = 8 - 5 = 7 - 4 have the same difference				
Represent and use number bonds and related subtraction facts	Concrete: Link to addition- use the part-part whole model to model the inverse.				
within 20.	Pictorial: Use pictorial representation to show the parts.				
	Abstract: Move to using numbers within the part-whole model.				
	5 4-1-0 7				

YEAR 1 - MULTIPLICATION

Objective:	CPA:				
Doubling numbers.	Concrete: Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling. Double 4 is 8 Pictorial: Draw pictures to show how to double numbers. Abstract: Partition a number and then double each part before recombining it back together. $10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\$				
Counting in multiples. (skip counting)	The representation for the amount of groups supports pupils' understanding of the written equation. Eg two groups of 2 are 2.4. Or five groups of 2 are 2.4.8,8,10. Number lines can be used in the same way as the bead string Concrete: Count the group as children are kip counting, children may use their fingers to help. Pictorial: Children make representations to show counting in multiples. Abstract: Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30				



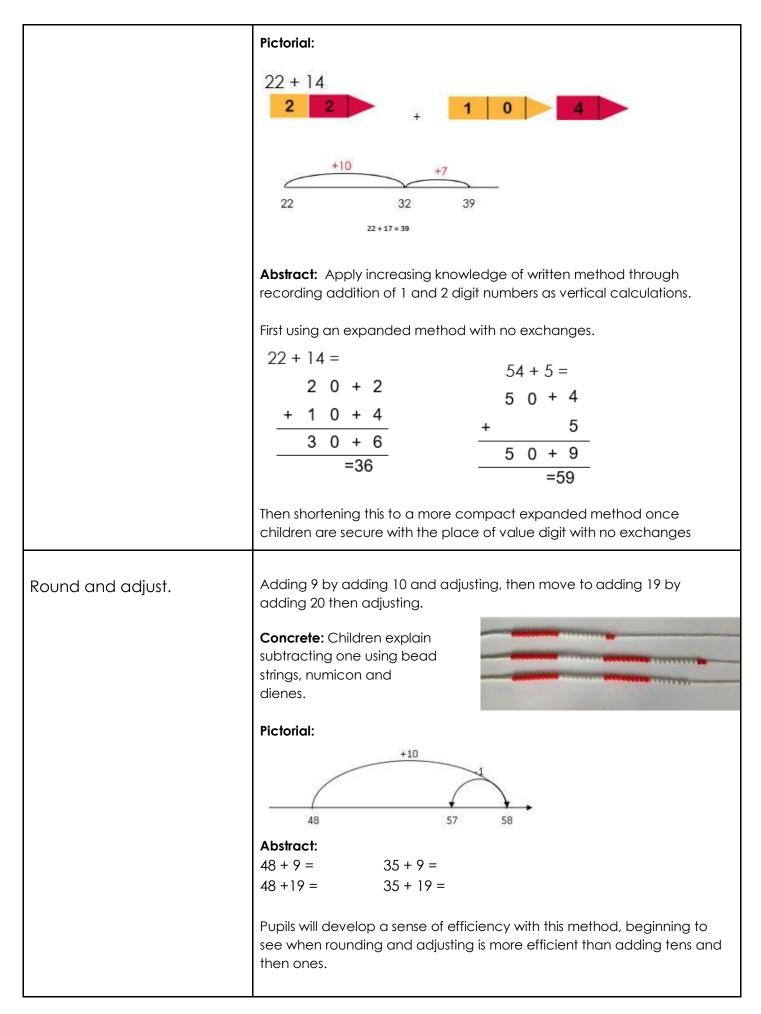
YEAR 1 - DIVISION

Division as sharing Concrete: Sharing using a range of objects: 6÷2= ↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓↓	Objective:	CPA:				
should also be encouraged to use their 2 times tables facts. To progress further, children can then be moved onto: '6 shared between 2 is 3'		Concrete: Sharing using a range of object 6 ÷ 2 = Image: Sharing using a range of object 6 ÷ 2 = Image: Sharing using a range of object 6 ÷ 2 = Image: Sharing using a range of object 6 ÷ 2 = Image: Sharing using a range of object 6 ÷ 2 = Image: Sharing using a range of object Image: Sharing using using a range of object Image: Sharing using				

YEAR 2 - ADDITION

Objective:	CPA:
Use known number facts including different combinations of tens & ones of any 2 digit number. Part-part-whole.	 Pupils explore the different ways of making 20. They can do this with all numbers using the same representations. Concrete: Children to explore ways to make numbers. Pictorial: This model develops knowledge of the inverse relationship between addition and subtraction and is used to find the answer to missing number problems.
	20PartPart $+ = 20$ $20 - = =$? $+ = 20$ $20 - = =$ 4 $+ = 20$ $20 - = =$ 4 $Abstract:$ Include teaching of
	the inverse of addition and subtraction: $16 - 1 = 1$ $1 + 1 = 16$ $16 - 1 = 1$
Adding multiples of ten.	Concrete: Model using dienes and bead strings. 50 = 30 + 20
	Exploring that one's digit does not change. Pictorial: Use representations for base ten.
	3 tens + 5 tens = tens 30 + 50 =

	$\begin{array}{r} +10 \\ \hline & +10 \\ \hline & & +$
Use known facts to create derived facts.	Concrete: Dienes blocks should be used alongside pictorial and abstract representations when introducing this strategy. Pictorial: Children draw representations of H, T & O. $ \begin{array}{c} $
Partitioning one number, then adding tens and ones	Concrete: Model using dienes, place value counters and numicon. 22 + 17 = 39 Pupils can choose themselves which of the two numbers they wish to partition. Pupils will begin to see when this method is more efficient than adding tens and taking away the extra ones, as shown. Use arrow cards and place value materials to partition (and part partition) numbers into tens and units to add.

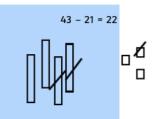


YEAR 2 - SUBTRACTION

Objective:	CPA:			
Subtracting tens and ones.	In year 1 pupils have been taught to partition the second number for this strategy as partitioning both numbers can lead to errors if regrouping is required.			
	Children begin subtracting ones from a two digit number. Then move on to subtracting tens before subtracting tens and ones			
	$34 \cdot 6 = 28$ $-1 -1 -1 -1 -1 58 \cdot 30 = 28$ $-10 -10 -10$ $28 29 30 31 32 33 34$ $28 38 48 58$			
	Concrete: Pupils use bead strings, numicon, dienes or other objects to explore subtracting two digit numbers from two-digit numbers.			
	Pictorial: Then combining these (in conjunction with using a hundred square to show jumps in tens and ones)			
	76 - 45 = 31 $-1 -1 -1 -1 -1 -1 0 -10 -10 -10$ $-2 -10$ $41 -43 -53$ $-1 -1 -1 -1 -1 -1 -1 -1 -1 -1 -10 -10$ $-10 -10 -10$ $-10 -10 -10$ $-$			
	Abstract: 76 - 45 =			
Partitioning to subtract - without regrouping. (friendly numbers)	Concrete: Use dienes to show how to partition the number when subtracting without regrouping. 34 - 13 = 21			

Pictorial: Children draw representations of dienes and cross off.

Abstract: Applying increasing knowledge of written method through recording subtraction of 1 and 2 digit numbers as vertical calculations.

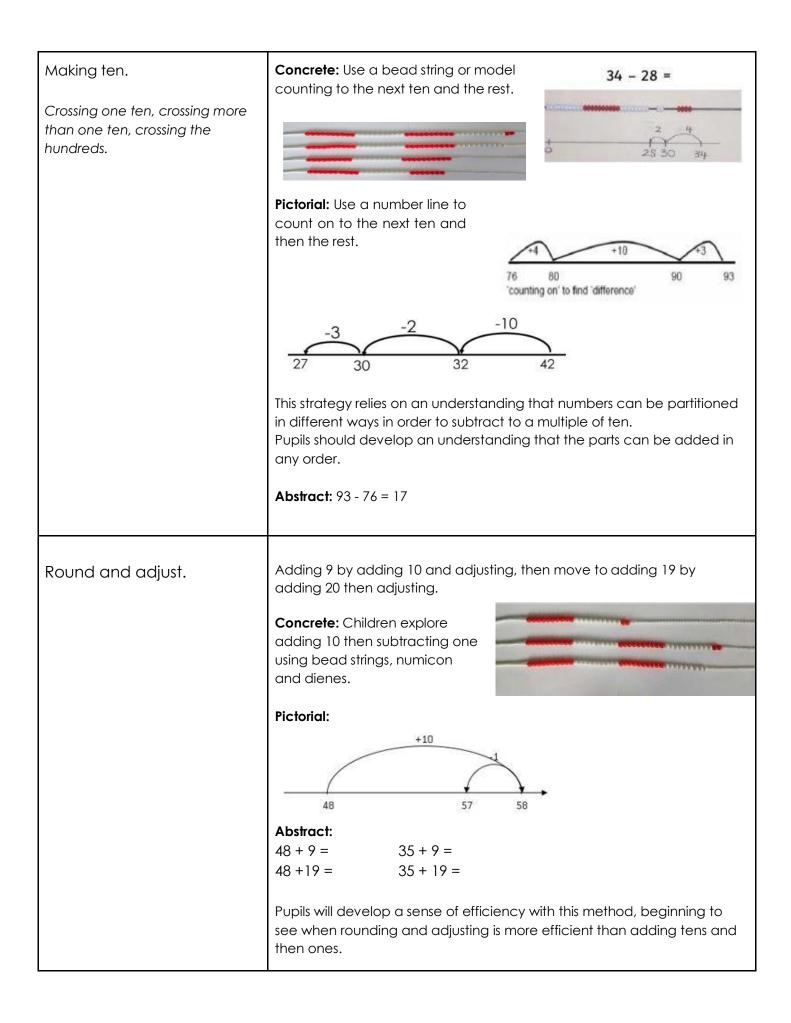


First using expanded method (with no regrouping)) 78 - 3 =

/0 0					
		7	0		8
	-				3
		7	0		5
			:	=75	
54 - 12 =					
5	0		4		
- 1	0		2		
4	0		2	_	
		=	42		

Moving to a compact method, once children are secure with the value of each digit (with no crossing the boundaries/regrouping)

	78	5	4
-	3	- 1	2
	7 5	4	2



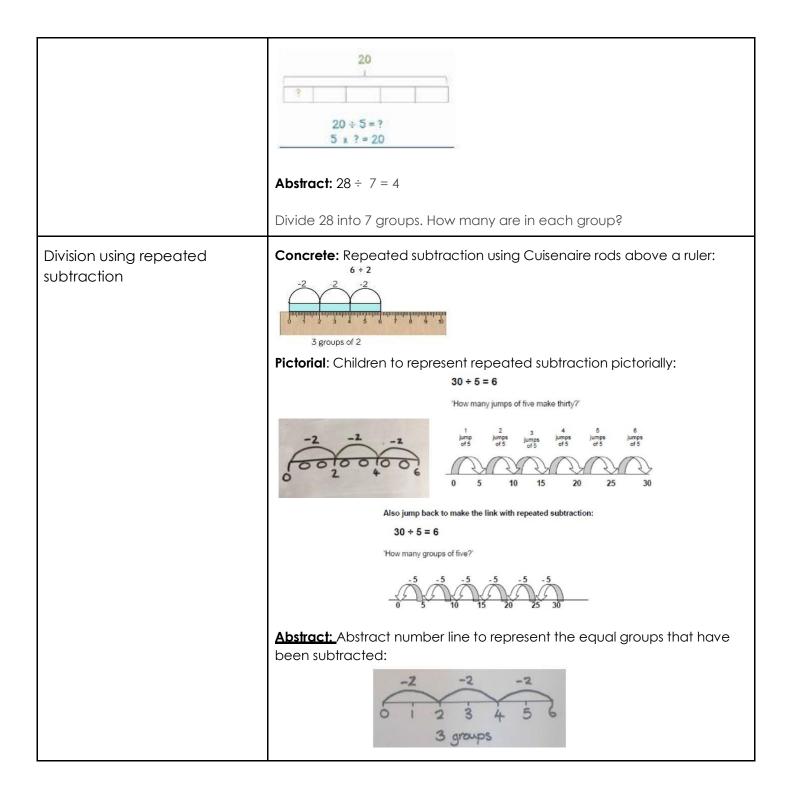
YEAR 2 - MULTIPLICATION

Objective:	CPA:		
Counting in multiples of 2, 5 and 10 from 0 (skip counting and repeated addition)	Pupils can use their fingers as they count to develop an understanding of 'groups of'. Concrete: Count the groups as children skip counting, children may use their fingers to help. Progress onto bar models. Pictorial: Number lines, counting sticks and bar models should be used to show representations of counting in multiples. Abstract: Count in multiples of a num aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15, 0, 5, 10, 15, 20, 25, 30		
Multiplication is commutative - arrays to represent multiplication equations	Concrete: Create arrays using counters, cubes and numicon. Image: Concrete: Create arrays using counters, cubes and numicon. Image: Concrete: Create arrays using counters, cubes and numicon. Image: Concrete: Create arrays using counters, cubes and numicon. Image: Concrete: Create arrays using counters, cubes and numicon. Image: Concrete: Create arrays using counters, cubes and numicon. Pupils should understand that an array can represent different equations and that as multiplication is commutative, the order of the multiplication does not change the answer. Image: Concrete: Concr		

	Use an array to write multiplication sentences and reinforce repeated addition. $5+5+5=15$ $3+3+3+3=15$ $5 \times 3 = 15$ $3 \times 5 = 15$ Abstract: 12 = 3 × 4 3 × 4 = 12 12 = 4 × 3 3 × 4 = 12
Using the inverse	This should be taught alongside division, so pupils learn how the two operations work alongside each otherConcrete: Children use numicon, cubes or other objects to find out how division and multiplication work alongside each other. Concrete: Children use numicon, cubes or other objects to find out how division and multiplication work alongside each other. Pictorial: Use the inverse triangle to create number sentences. Abstract: Show all 8 related fact family sentences.Abstract: Show all 8 related fact family sentences. $2 \times 4 = 8$ $8 = 2 \times 4$ $4 \times 2 = 8$ $8 = 4 \times 2$ $8 \div 2 = 8$ $2 = 8 \div 4$ $8 \div 4 = 2$ $4 = 8 \div 2$
Doubling numbers.	At this stage they double the 2x table facts to derive the 4x table facts. Concrete: Model doubling using dienes and place value counters. Pictorial: Draw pictures and representations to demonstrate how to double numbers. Abstract: Partition a number and then double each part before recombining it back together. $\int 5 \times 2 = 10$ $\int 5 \times 4 = 20$ $\int 5 \times 4 = 20$ $\int 5 \times 4 = 20$

YEAR 2 - DIVISION

Objective:	CPA:
Division as sharing	Concrete: I have 10 cubes, can you share them into 2 equal groups? 10 10 10 10 10 10 10 10 10 10
	Abstract: 12 ÷ 3 = 4
Division as grouping	Concrete: Divide quantities into equal groups. Use cubes, counters, objects or place value counters to air understanding.
	Pictorial: Use number lines for grouping:
	Use bar model to support with division:



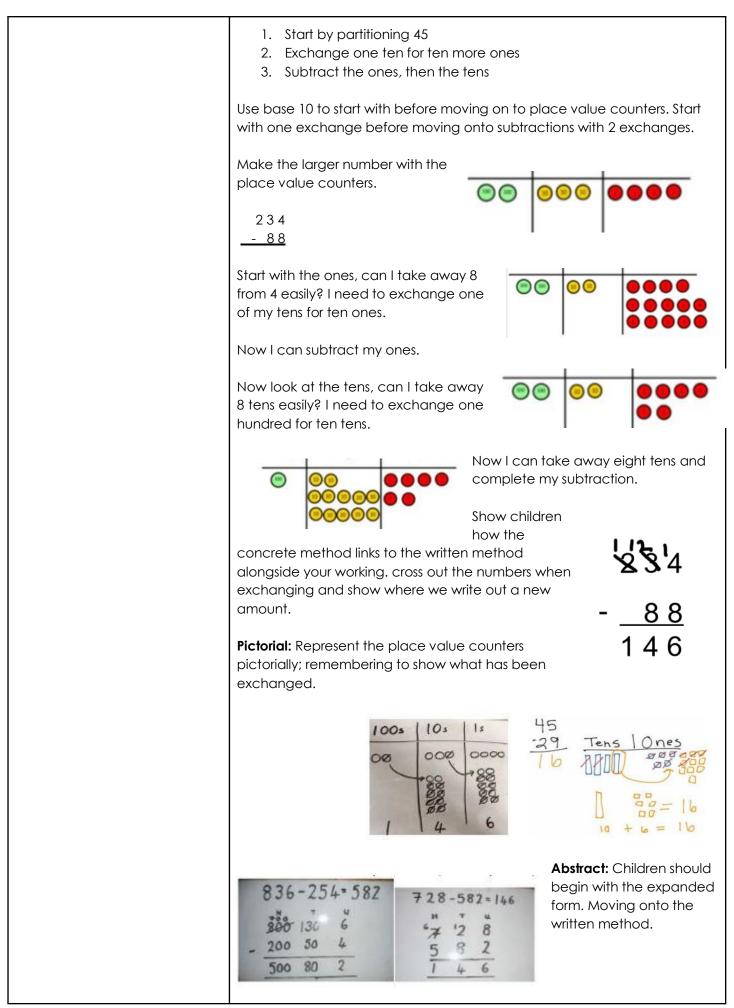
YEAR 3 - ADDITION

Objective:	CPA:			
Add 1 digit number to a 2 or 3 digit number.	Refer to Year 3 Addition Calculation policy			
Column Addition- no regrouping (friendly numbers) (Up to 3 digit numbers)	Concrete: Add together the ones first then add the tens. Children to partition the number 'How many tens do we have? How many ones do we have?' 63 + 32 = 95 6 tens is 60 and 3 ones 3 tens is 30 and 2 ones $+ \frac{30 + 2}{90 + 5} = 95$ Use the Base 10 blocks first before moving onto place value counters. Pupils should be encouraged to use known facts to derive answers, rather than relying on counting manipulative or images. e.g. 'I know 2 + 1 = 3 so 2 tens plus 1 ten is equal to 3 tens which is 30. T 0 one of the second sec			
	Pictorial: After practically using the base 10 blocks and place value counters, children can draw the counters to help them solve additions. T O O O O O O O O O O O O O O O O O O			

Column Addition- with regrouping	Concrete: Make both numbers on a place value grid. 146 + 527 =				
	1 hundreds 4 tens and 6 ones 100 + 40 + 6				
(Up to 3 digit numbers)	5 hundreds 2 tens and 7 ones 500 + 20 + 7				
	Image: Second				
	Add up the rest of the columns,				
	exchanging the 10 counters				
	from one column for the next + 527				
	place value column unfil every				
	column has been added.				
	This can also be done with Base 10 to help children clearly see that 10 ones is equal to 1 ten and the 10 tens equal 100.				
	As children move on to decimals, money and decimal place value,				
	counters can be used to support learning.				
	Pictorial: Children can draw a pictorial				
	representation of the columns and place				
	value counters to further support their				
	learning and understanding.				
	Abstract: Children follow written steps to regroup and form calculations correctly. 6 7 3				
	As the children move on,				
	As the children move on, introduce decimals with				
	H T O Always start in the ones the same number of				
	decimal places and				
	1 4 6 different. Money is used				
	+ 5 2 7 for context.				
	6 7 3				
	72.8 £ 2 3 . 5 9				
	$\frac{+54.6}{127.4} \qquad \qquad$				
	11				
	9 . 0 8 0 5 9 . 7 7 0				
	+ 1 . 3 0 0				
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
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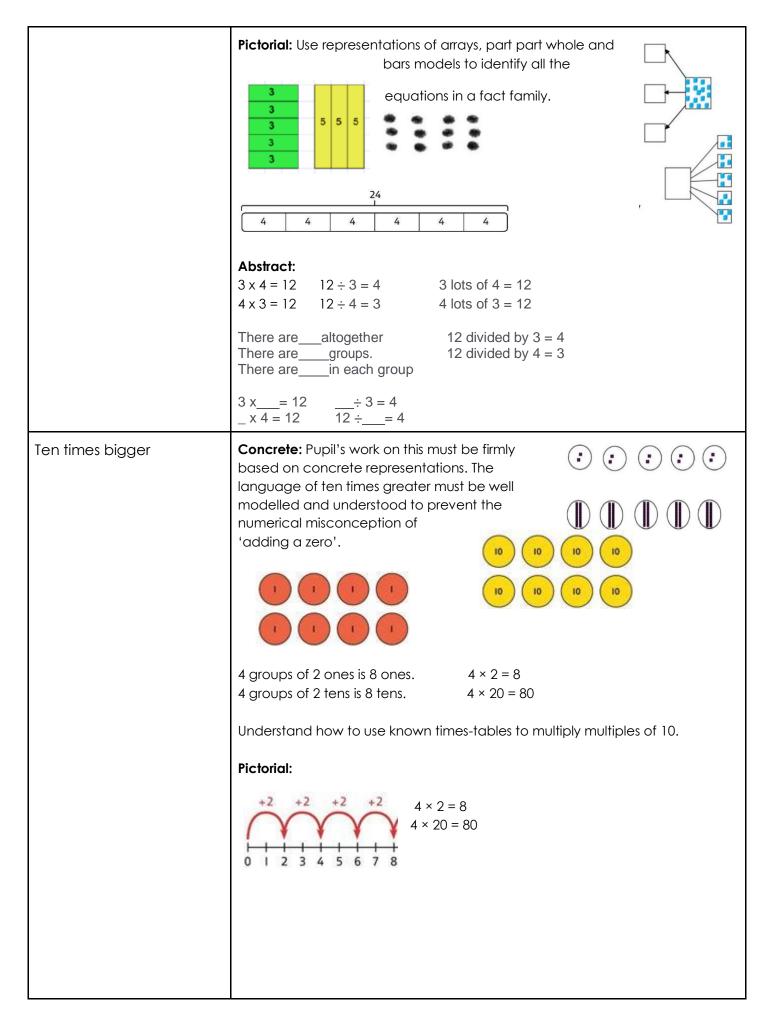
YEAR 3 - SUBTRACTION

Objective:	CPA:			
Column subtraction - without exchanging.	Concrete: Column method using base ten or numicon.			
(friendly numbers)	Subtract the ones first then subtract the tens.			
	Children to partition the number 'How many tens do we have? How many ones do we have?' 47 + 32 = 4 tens is 40 and 7 ones $40 + 7$ 3 tens is 30 and 2 ones $-30 + 2$			
	10 + 5 = 15 Use the Base 10 blocks first before moving onto place value counters and numicon. Pupils should be encouraged to use known facts to derive answers, rather than relying on counting manipulative or images. e.g. 'I know 4 - 3 = 1 so 4 tens take away 3 tens is equal to 1 tens which is 10.'			
	Pictorial: Children to represent the base 10 pictorially- crossing out the ones, then the tens.Image: Children to represent the base 10 pictorially- crossing out the ones, then the tens.Image: Children to represent the base 10 pictorially- crossing out the ones, then the tens.Image: Children to represent the base 10 pictorially- crossing out the ones, then the tens.Image: Children to represent the base 10 pictorially- crossing out the ones, then the tens.Abstract: ChildrenShould begin with the expanded form before moving on to the formal written method.Children use written steps to format the question correctly.268 - 124 = 200 + 60 + 8 $100 + 20 + 4$ Image: Children to the format the question correctly.Content the format the question correctly.			
Column subtraction - with exchanging	Concrete: Begin with base 10 or Numicon. Move to place value counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange. Column method (using base 10 and having to exchange) 45 - 26			



YEAR 3 - MULTIPLICATION

Objective:	CPA:				
Doubling to derive new multiplication facts	Concrete: Pupils continue to make use of the idea that facts from easier times tables can be used to derive facts from related times tables using doubling as a strategy. This builds on the doubling strategy from year 2. Pictorial: Draw pictures and arrays to support understanding $3 \times 9 = 3 \times 6 = \text{double } 9 = 3 \times 2 = 6$ $3 \times 2 = 6$ $3 \times 4 = 12$ $3 \times 8 = 24$ What is 6×8 ? How do you know this?				
Counting in multiples of 2, 3, 4, 5. 6, 8 and 10 (skip counting and repeated addition)	Refer to Year 2 multiplication calculation policy. Rehearsal of previously learnt tables from Year 2 as well as new content for Year 3 should be incorporated into transition activities and practised regularly. 6 lots of 4 4, 8, 12, 16, 20, 24 4 + 4 + 4 + 4 + 4 + 4 8 lots of 3 8 groups of 3 3, 6, 9, 12, 15, 18, 21, 24 3 + 3 + 3 + 3 + 3 + 3 + 3 =				
Multiplication is commutative (part part- whole model, arrays and bar model to establish commutativity and inverse relationship between multiplication and division)	 Refer to Year 2 multiplication calculation policy. Concrete: Pupils continue to use arrays with counters, cubes and numicon. Use blank Part-Part-Whole and move manipulatives. Use language structures and encourage children to use. E.g 1 group of 3, 2 groups of 3, 3 groups of 3, 4 groups of 3 make 12 12 has been shared equally into 4 groups I have 3 in each group. 4 groups of 3 make 12. 				

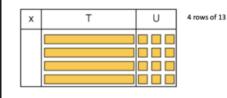


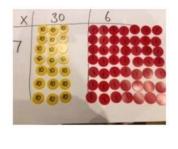
Multiplying 2 digit number by 1 digit number

(Grid method- partitioning)

Concrete

Show the links with arrays to first introduce the grid method.





4 rows of 10 4 rows of 3

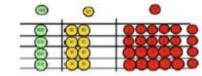
Move on to using Base 10 to move towards a more compact method.

Move onto place value counters to show how we are finding groups of a number. Add up each column, starting with the

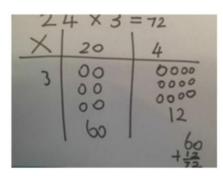
ones making any exchanges needed. The calculation will be shown alongside the model chosen to see the connection. e.g. 36 x 7

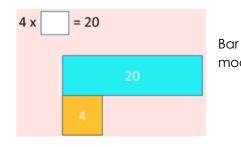
Ensure you make it clear if you are multiplying by 7 you will need 7 rows. If you are multiplying by 4, show 4 rows





Pictorial: Children can represent their work with place value counters in a way that they understand. They can draw the counters using colour to show different amounts or just use the circles in the different columns to show their thinking.

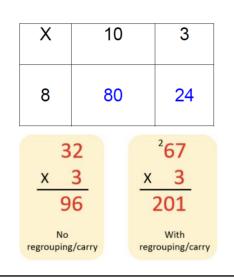




Abstract: Begin with multiplying by one digit numbers and showing the clear addition alongside.

Introduce formal written method

models are used to explore missing numbers



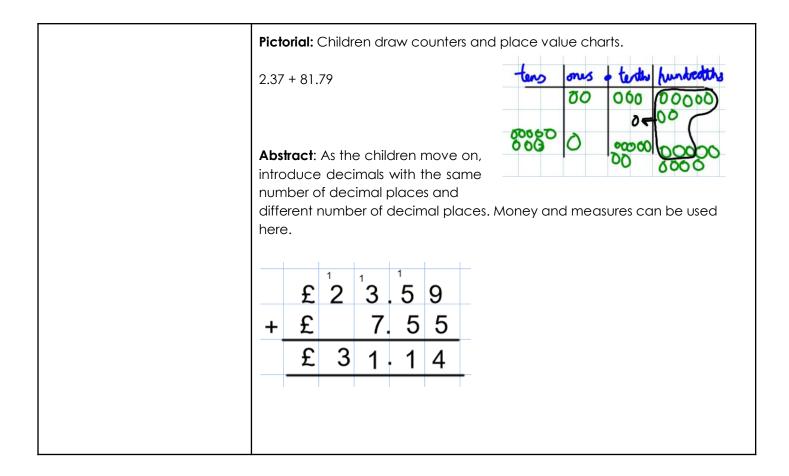
YEAR 3 - DIVISION

Objective:	CPA:
Using times-tables knowledge to divide (Make equal groups)	Use knowledge of known times-tables to calculate divisions. I'need to work out 30 shared between 5. Concrete: Children use numicon, cubes or other manipulatives to show groups of 3 or 3 groups of 5. As the children to share them equality from known multiplication facts I know that $3 \times 5 = 15$ so I know that $15 \div 3 = 5$. Pictorial: A bar model may represent the relationship 24 $24 \div 4 = 6$ $24 \div 4 = 6$ $24 \div 6 = 4$ Children understand how division is related to both repeated subtraction and repeated addition. $\sqrt{-4 + 4 = 6}$ $24 \div 6 = 4$ Children understand how division is related to both repeated subtraction and repeated addition. $\sqrt{-4 + 4 = 6}$ $4 \pm 6 = 4$ Children understand how division is related to both repeated subtraction and repeated addition. $\sqrt{-4 + 4 = 6}$ $4 \pm 6 = 4$ Children understand how division is related to both repeated subtraction and repeated addition. $\sqrt{-4 + 4 = 6}$ $4 \pm 6 = 4$ Datate: How on to sentence structures of knowing fact families. Lindauce formal written method to support the number sentence. $\sqrt{4 + 24}$ $4 \pm 4 \pm 4 \pm 4$ $4 \pm 4 \pm 4 \pm 4$ 4 ± 4

Division with arrays	Concrete: Link division to multiplication by creating an array and thinking				
	about the number sentences that can be				
	created.				
	$15 \div 3 = 5$ $5 \times 3 = 15$				
	$15 \div 5 = 3$ $3 \times 5 = 15$				
	Pictorial Dansaction data di se				
	Pictorial: Draw an array and use lines				
	to split the array into groups to make				
	multiplication and division sentences.				
	$15 \div 3 = 5$ $5 \times 3 = 15$				
	$15 \div 5 = 3$ $3 \times 5 = 15$				
	Abstract: Find the inverse of				
	multiplication and division sentences by creating eight linking number sentences:				
	semences.				
	7 x 4 = 28				
	28 ÷ 7 = 4 28 ÷ 4 = 7				
	28 = 7 x 4 28 = 4 x 7				
	$4 = 28 \div 7$ $7 = 28 \div 4$				
Division with remainders	Concrete: This can be done with				
	Iollipop sticks or Cuisenaire rods:				
	13 ÷ 4				
	Use of lollipop sticks to form whole-				
	squares are made because we				
	are dividing by 4.				
	There are 3 whole squares, with 1 left over.				
	Pictorial : Children represent the Iollipop sticks pictorially.				
	There are 3 whole				
	squares, with 1 left				
	75				
	Abstract: $13 \div 4 = 3$ remainder 1				
	Children should be encouraged to use their times table facts; they could				
	also represent repeated				
	addition on a number line.				
	3 groups of 4, with 1 left				
	over				

YEAR 4 - ADDITION

Formal written method- with and written method- written method regrouping Refer to Year 3 addition calculation policy. Break down into necessary steps needed. e.g. Add two 3 digit numbers - nor arrosing 10 or 100 Add two 4 digit numbers - nor arrouping Add two 4 digit numbers - nor arrouping (up to 4 digit numbers) IO0 Add two 4 digit numbers - nor arrouping Add two 4 digit numbers - nor arrouping Concrete: Continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. The calculation to be shown alongside the manipulatives used to see the connection. Use place value counters to calculate 455 + 456 exchanging ten ones for a thousand . Pictorial: Draw representations using place value grid. Number sentences and formal written methods are also shown. Image: ten one of the sentences and formal written methods are also shown. Pictorial: Draw representations using place value grid. Number sentences and formal written methods are also shown. Image: ten one value grid. Number sentences and formal written methods are also shown. Pictorial: Draw representations using place value grid. Number sentences and formal written method. Continue from previous work to carry hundreds as well as tens. Relate to money and measures. Image: ten one value grid. Number sentences and formal written retainship between these. Place value grid. Shown. All of the calculation strategies for integers (whole numbers) can be used to build a conceptual understanding of the relationship between these. Place value grid. The greatest and the relationship between these. Place value grid. The	Objective:			CPA:					
be shown alongside the manipulatives used to see the connection. $\overline{1}$	and without regrouping	 Refer to Year 3 addition calculation policy. Break down into necessary steps needed. e.g. Add two 3 digit numbers - not crossing 10 or 100 Add two 4 digit numbers - no regrouping Add two 3 digit numbers- crossing 10 or 100 Add two 4 digit numbers- one regroup Add two 4 digit numbers- more than one regrouping Concrete: Continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. 							
Calculating with decimals (Up to 2 dp) Assign different values to dienes equipment. These can then be used to build a conceptual understanding of the relationship between these. Place value counters are another useful manipulatives for representing decimal numbers.								F	F
used to see the connection. Image: set the connection. I		-	0000	000			125	200.004	5
Pictorial: Draw representations using place value grid. Number sentences and formal written methods are also shown. 7 1 5 Abstract: Formal written method. Continue from previous work to carry hundreds as well as tens. Relate to money and measures.		used to see the	0000	000		+	4	3	6
(Up to 2 dp) All of the calculation strategies for integers (whole numbers) can be used to calculate with decimals. Concrete: Introduce decimal place value		Abstract: Formal wri previous work to ca	writte	Continue fro	ore also show $\frac{1}{2}$ + 4 om 7	wn.	3 4	4 7 1	
counters and model exchange for addition.	(Up to 2 dp) All of the calculation strategies for integers (whole numbers) can be	equipment. These conceptual relationship between counters are another for representing deconception Concrete : Introduce	an then be us understandin n these. Place er useful mani simal numbers e decimal pla	g of the e value pulatives s. ce value	tens ones			e = 0.	



YEAR 4 - SUBTRACTION

Objective: CPA:				
Formal written method- with and without exchanging (Up to 4 digit numbers)	Refer to Year 3 subtraction calculation policy. Break down into necessary steps needed. e.g. Subtract a 3 digit number from a 3 digit number- no exchange Subtract two 4 digit numbers- no exchange Subtract a 3 digit number from a 3 digit number- exchange Subtract two 4 digit numbers- one exchange Subtract two 4 digit numbers- more than one exchange Subtract two 4 digit numbers- more than one exchange Concrete: Model process of exchange using numicon, base ten and then move to place value counters. Ensure the calculation is shown alongside the modern chosen.			
	Pictorial: Children to draw place value counters and bar modelling and show their exchange- see Y3 Use bar modelling to support children with word problems Abstract: Formal written method. Children must understand what has happened when they have crossed out digits see Y3 What happens when you can't subtract 9 ones from 7 ones? What do we need to do? What do we exchange? When do we exchange?			

Calculating with decimals- with and without exchanging	Refer to Year 3 subtraction calculation policy and Year 4 addition calculation policy for CPA examples.
(Up to 2 dp)	In the context of money and measure.
All of the calculation strategies for integers (whole numbers) can be used to calculate with decimals	

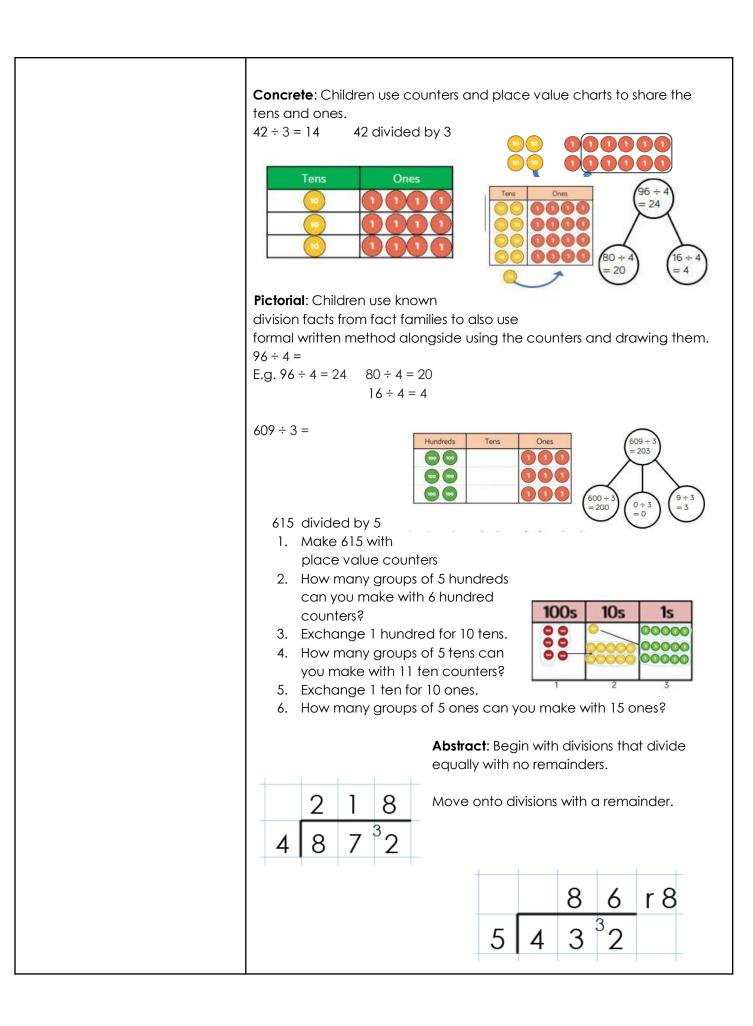
YEAR 4 - MULTIPLICATION

Objective:	CPA:
Objective: Multiplying by multiples of 1, 10, 100.	CPA: Concrete: Use place value resources, dienes and counters to understand how to multiply by multiples of 1, 10 and 100. When you multiply by ten, each part is ten times greater. The ones become tens, the tens become hundreds, etc. When multiplying whole numbers, a zero holds a place so that each digit has a value that is ten times greater. Repeated multiplication by ten will build an understanding of multiplying by 100 and 1000. Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution Solution
Times table knowledge up to 12 x 12	$40 \times 7 = 280$ $400 \times 7 = 2,800$ Concrete: Understand the special cases of multiplying
	by 1 and 0. Children use any resources to show the children the difference between x 1 and x 0.
	$5 \times 1 = 5 \qquad \qquad 5 \times 0 = 0$

	Use numicon, counters or counters to represent the relationship between the times tables. E.g. x9 and x10	
	*11 table and ×12 tables in relation to the ×10	
	table. $2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 11 = 40 + 4$ $4 \times 12 = 40 + 8$	
	Pictorial: To support concrete children to draw the cubes, using colours.	
	Abstract : Move children on to writing full number sentences and knowing their times table mentally. Children being able to explain methods for learning their times tables, the relationships and difference between some multiplication facts.	
Formal written method- Multiplying 2 digit and 3 digit numbers by 1 digit number	Refer to Year 3 multiplication calculation policy to consolidate grid method with partitioning. Use same methods to solve 3 digit numbers by 1 digit numbers before moving on to formal written method.	
	Concrete: Use place value counters to make the 3 digit number then repeat this by the number you are multiplying by.	
	Make 4 × 136 using equipment. I can work out how many 1s, 10s and 100s.	
	There are 4 × 6 ones 24 ones	
	There are 4 × 3 tens 12 tens	
	There are 4 × 1 hundreds 4 hundreds	
	Pictorial: Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit. Refer back to the grid method and allow children to discover the connection. Abstract: Children use formal written method with and without	
	regrouping.	

YEAR 4 - DIVISION

Objective:	CPA:	
Dividing by multiples of 1, 10	Refer to Year 4 multiplication calculation policy for CPA. When you divide by ten, each part is ten times smaller. The hundreds become tens and the tens become ones. Each digit is in a place that gives it a value that is ten times smaller. When dividing multiples of ten, a placeholder is no longer needed so that each digit has a value that is ten times smaller. E.g. $210 \div 10 = 21$	
and 100.		
	Concrete: Use dienes, place value charts and counters to show what is happening to each digit.	
	90 + 3 = 90 + 3 = 900 + 3 = 900 + 3 =	3 ÷ 1 = 3 30 ÷ 10 = 3 300 ÷ 100 = 3
		300 ÷ 10 = 30 3000 ÷ 100 = 30
	Pictorial: Encourage children to draw the place value chart and show what is happening to each digit to support the use of concrete resources.	3000 ÷ 10 = 300
	Abstract: Use known facts and understanding commutativity to multiply mentally. Emphasis is placed on understanding the relat times smaller) between a known number fact allowing far larger 'fact families' to be derived number fact. $9 \div 3 = 3$ 9 tens divided by 3 is 3 tens. 9 hundreds divided by 3 is 3 hundreds.	ionship (10 times or 100 and one to be derived,
Formal written method- short division	Refer to Year 1 and 2 division calculation polic Year 3 division calculation policy to consolida	-
(Up to 3-digit by 1-digit)	Children divide 2-digit numbers by a 1-digit numbers and ones and sharing into equal groups. involve exchanging between the tens and or when consolidated.	They divide numbers that
	Then move on to 3-digit numbers by 1-digit nu	mbers. rem



YEAR 5 - ADDITION

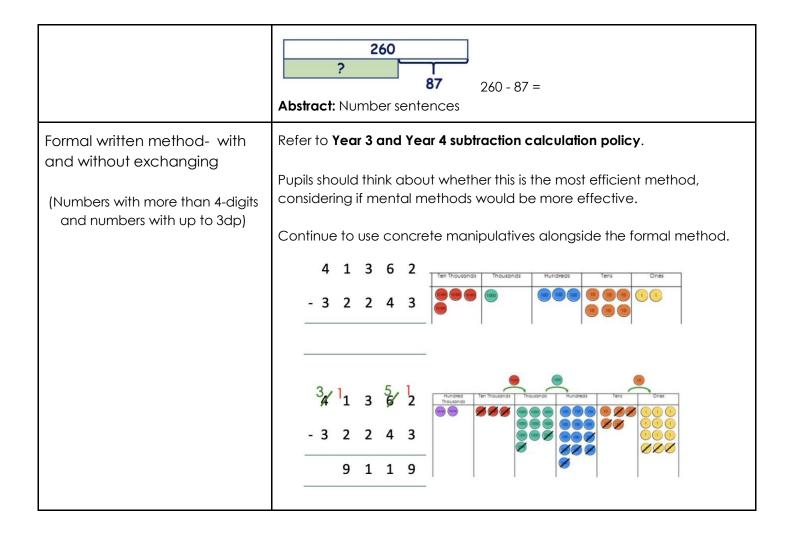
Objective:	CPA:	
Count forwards or backwards in steps of powers of 10 for any given number up to 1,000,000	Work with numbers up to 1,000,000 as well as tenths, hundredths and thousandths.	
Adding and subtracting	Concrete: place value counters on a place value chart, repeatedly adding the same counter and regrouping as needed. Image: transit transi transit transit tran	
	backwards. Abstract: Children write number sentences. Pay particular attention to boundaries where regrouping happens more than once and so more than 1-digit changes. e.g. 9,900 + 100 = 10,000 or 99,000 + 1,000 = 100,000	
Using known facts and understanding of place value to derive. (multiples of 10 000 and 100 000 as well as tenths, hundredths and thousandths) Adding and subtracting	Using the following language makes the logic explicit: I know three ones plus four ones is equal to seven ones. Therefore, three ten thousands plus four ten thousands is equal to seven ten thousands. Concrete: $3 + 4 = 7$ $30\ 000 + 40\ 000 = 70\ 000$ $300\ 000 + 400\ 000 = 700\ 000$ $0\ 1\ +\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0\$	
	60000 Fictorial: Encourage use of part-part-whole as well as drawing counters. 20 000 + 20 000 = 60 000 60 000 60 000 - 40 000 = 20 000 60 000 60 000 - 20 000 + 40 000 60 000	

	0.6 = 0.2 + 0.4 0.6 = 0.4 + 0.4 0.2 = 0.6 - 0.4 0.4 = 0.6 - 0.2 Abstract: Number sentences.	
Partitioning one number and applying known facts to add.	Partitioning into place value amounts (canonical partitioning) Concrete: Use place value counters to represent the larger number and then add each place value part of the other number.	
	4650 + 7326 = 7326 + 4000 + 600 + 50 Pictorial: Represent on empty number line. Extend the 'Make ten' strategy (See Y1 and Y2 addition) to count on to multiple of 10. Partitioning in different ways (non-canonical partitioning) $\frac{+15}{6785} + 200 + 4000}{7000} + 4000 + 50$ The strategy can be used with decimal numbers. 14.7 + 3.6 = 14.7 + 0.3 + 3.3 = 15 + 3.3 = 15 + 3.3 + 0.3 + 3.6 + 3.	
Formal written method- with and without regrouping. (Numbers with more than 4-digits and numbers with up to 3dp)	Refer to Year 3 and Year 4 addition calculation policy.Pupils should think about whether this is the most efficient method, considering if mental methods would be more effective.Continue to use concrete manipulatives alongside the formal method.When adding decimal numbers with a different number of decimal places, in order to avoid calculation errors, pupils should be	

encouraged to insert zeros so that there is a digit in every row. This is not necessary for calculation and these zeros are not place holders as the value of the other digits is not changed by it being placed. 34.25 15.4 $+ \frac{6.362}{56.012}$ 34.250 15.400
+ 06.362 <u>56.012</u>

YEAR 5 - SUBTRACTION

Objective:	CPA:	
Using known facts and understanding of place value to derive.	Refer to Year 5 addition Calculation Policy. 75 221 - 14 300 = 75 221 - 10 000 - 4000 - 300	
(multiples of 10 000 and 100 000 as well as tenths, hundredths and thousandths)		
Adding and subtracting		
Subtracting by partitioning and applying known facts.	Partitioning into place value amounts (canonical partitioning) Concrete: Use place value counters to represent the larger number. Pictorial: Represent on an empty number line starting on the right and having the arrows jump to the left -300 -4000 -10 000 60 921 61 221 65 221 75 221 Develop understanding that the parts can be subtracted in any order and the result will be the same. -10 000 -300 -4000 60 921 70 921 71 221 75 221 Partitioning in different ways (non-canonical partitioning) Extend the 'Make ten' strategy (see guidance in Y1 or Y2) to count back to a multiple of 10. Use Bar models represent subtractions in problem contexts, including 'find the difference'. Explain the mistake made when the columns have not been ordered correctly. Use approximation to check calculations. 'I calculated 18,000 + 4,000 mentally to check my subtraction.'	



YEAR 5 - DIVISION

Objective:	CPA:	
Dividing whole and those involving decimals by 10, 100 and 1,000	Refer to Year 3 and 4 division calculation policy and introduce dividing by 1,000 in the same CPA way. Introduce dividing numbers that involve decimals by 10, 100 and 100. When you divide by ten, each part is ten times smaller. The hundreds become tens and the tens become ones. Each digit is in a place that gives it a value that is ten times smaller. When dividing multiples of ten, a placeholder is no longer needed so that each digit has a value that is ten times smaller. E.g. 210 ÷ 10 = 21 210.3 ÷ 10 = 21.03	
Formal written method- short division (Up to 4-digit by 1-digit)	Refer to Year 4 division calculation policy and introduce dividing 4-digit by 1-digit in the same CPA way. Interpret remainders appropriately for the context. Children can then progress onto expressing the remainder as fractions (e.g. 5/8) and decimals (e.g. 663.625).	
The thought process of the traditional algorithm is as follows: How many 4s in 8? 2 How many 4s in 5? 1 with 1 remaining so regroup. How many 4s in 12? 3 How many 4s in 8? 2 Warning: If you simply apply place value knowledge to each step, the	Concrete: Sharing: 8 thousands shared into 4 equal groups 5 hundreds shared into 4 equal groups Regroup 1 hundred for 10 tens 12 tens shared into 4 equal groups 8 ones shared into 4 equal groups. Sharing the dividend builds conceptual understanding however doesn't	
thinking goes wrong if you have to regroup. How many 4s in 8000? 2000 How many 4s in 500? 100 with 1 remaining (illogical) The answer would be 125.	shalling the dividend bolids conceptibli of defision differentiating nowever doesn't scaffold the "thinking" of the algorithm. Using place value counters and finding groups of the divisor foreach power of ten will build conceptual understanding of the short division algorithm. <u>Groupina:</u> How many groups of 4 thousands in 8 thousands? How many groups of 4 hundreds in 5 hundreds? 2 1 3 2 4 8 512 8	

Regroup 1 hundred for 10 tens. How many groups of 4 tens in 12 tens? How many groups of 4 ones in 8 ones?
Pictorial : Children draw the place value chart and counters and show if they are grouping or sharing.
Abstract: Short multiplication with a clear understanding of regrouping. Using the language structures adobe to explain each step.

YEAR 5 - MULTIPLICATION

Objective:		CPA:
Multiplying whole and those involving decimals by 10, 100	Refer to Year 3 and 4 multin multiplying by 1,000 in the s	olication calculation policy and introduce ame CPA way.
and 1,000	100. When you multiply by ten, e become tens, the tens bec	pers that involve decimals by 10, 100 and each part is ten times greater. The ones come hundreds, etc. When multiplying whole ace so that each digit has a value that is ten $\frac{1}{10000000000000000000000000000000000$
Using Known facts and place value to derive multiplication facts.	Emphasis is placed on understanding the relationship (10 times or 100 times greater) between a known number fact and one to be derived, allowing far larger 'fact families' to be derived from a single known number fact. Knowledge of commutativity is further extended and applied to find a range of related facts Pupils should work with decimals with up to two decimal places. These derived facts should be used to estimate and check answers to calculations.	
	Concrete: Use place value to show different arrays- 2 x 3 x 2 = 6	
	2 x 30 = 60	
	30 x 2 = 60	
	2 x 300 = 600 300 x 2 = 600	2 x 30 x 10 = 600 20 x 3 x 10 = 600

	Pictorial: Children to draw place value counters to find larger fact families. Abstract: Number sentences. Multiplication facts pupils should be able to derive from known fact ² 100 000 ^{700 000 x3} ^{70 000 x30} ^{700 x 300} ^{70 x 3000} ^{70 x 30 000} ^{70 x 30 00} ^{70 x 30 00}	
Formal written method (Multiplying 2-digit, 3-digit by 2 digit number)	Refer to Year 3 and Year 4 multiplication calculation policy. Concrete: Extend the place value chart model used in Year 4, using an additional row on the place value chart. Pictorial: Children draw representation alongside the calculation.	
	2 4 3 12 4 8 6 0 2 4 3 0 0 0 0 <	

YEAR 6 - ADDITION

Objective:	CPA:
Count forwards or backwards in steps of powers of 10 for any given number up to 10,000,000	Refer to Year 5 addition calculation policy for CPA ideas for numbers up to 10 000 000.
Using known facts and understanding of place value to derive. (multiples of 10 000, 100 000 and 1 000 000 as well as tenths, hundredths and thousandths))	Refer to Year 5 addition calculation policy for CPA ideas for numbers up to 1 000 000
Partitioning one number and applying known facts to add.	Refer to Year 5 addition calculation policy for CPA.
Formal written method- with and without regrouping. (Numbers with more than 4-digits and numbers with up to 3dp)	Refer to Year 3, 4 and 5 addition calculation policy for CPA.

YEAR 6 - SUBTRACTION

Objective:	CPA:
Count forwards or backwards in steps of powers of 10 for any given number up to 10,000,000	Refer to Year 5 addition calculation policy for CPA ideas for numbers up to 10 000 000.
Using known facts and understanding of place value to derive.	Refer to Year 5 addition calculation policy for CPA ideas for numbers up to 1 000 000
(multiples of 10 000, 100 000 and 1 000 000 as well as tenths, hundredths and thousandths))	
Partitioning one number and applying known facts to add.	Refer to Year 5 addition calculation policy for CPA.
Formal written method- with and without regrouping.	Refer to Year 3 , 4 and 5 addition calculation policy for CPA.
(Numbers with more than 4-digits and numbers with up to 3dp)	

YEAR 6 - DIVISION

Objective:	CPA:
Dividing using formal written method- short division	Refer to Year 4 and Year 5 division calculation policy.
(Up to 4-digit by 1-digit)	
Dividing using formal written method- long division with and without remainders.	Follow the language structures of the short division strategy. Instead of recording the regrouped amounts as small digits the numbers are written out below. This can be easier to work with when dividing by larger numbers. $\begin{array}{c} 3 \ 4 \\ 12 \ 4 \ 0 \ 8 \\ 3 \ 6 \end{array}$
(4-digit by 2-digit)	48How many 12s go into 4, you can't do. 4 8Regroup the 4 which makes 40. 4 8How many 12s go into 40? 0 You can make 36 with 3 lots of 12. 0 Subtract 36 from 40 which leaves you with 4 tens. 0 Bring the 8 ones down which makes 48. 0 How many groups of 12 make 48? 0 You can make 4 groups of 12 which is 48. 48 subtracted from 48 is 0 so we have no remainder. $408 \div 12 = 34.$ $12 = 34.$ Move children on to larger numbers for the divisor.e.g. 8208 ÷ 24 24 How many 24s go into 8, you can't do.Regroup the 8 to make 82.How many 24s go into 8.2?Which multiple of 24 is closest to 82?You can make 72 which is 3 times with 10 remaining.Bring the 0 down to regroup 100.
	How many 24s go into 100? You can make 96 which is 4 lots of 24 with 4 remaining. Bring down the 8 to regroup 48. How many 24s make 48? 2 with no remainders. $\frac{-72}{100}$ $\frac{-96}{100}$ $\frac{-96}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-48}{100}$ $\frac{-240}{100}$

YEAR 6 - MULTIPLICATION

Objective:	CPA:
Formal written method (Multiplying 2-digit, 3-digit and 4-digit numbers by 1 digit number)	Refer to Year 4 and Year 5 multiplication calculation policy.
Formal written method (Multiplying 2-digit, 3-digit by 2-digit number)	Refer to Year 4 and Year 5 multiplication calculation policy.
Multiply decimals by integers	Refer to Year 3 and Year 4 multiplication calculation policy for CPA. Apply similar CPA for Decimals. Concrete: use counters and place value charts. Multiply 1.212 by 3 Pictorial: Use 100 square to show children multiplying a decimal by integer is similar on repeated addition. Multiply 4 x 0.2. This means 4 groups of two tenths. $4 \times 0.2 = 8$ 2×4 1.74 $\frac{x}{1522}$ $+ \frac{1740}{22.62}$